THE AUTHENTICITY OF ARCHYTAS FR. 1

In a long note in his epoch-making book on ancient Pythagoreanism Walter Burkert raised some grave doubts about the authenticity of Archytas Fr. 1 which have recently been challenged in an article by A. C. Bowen. In this paper I have two goals. First, I will evaluate Burkert's doubts and the success of some of Bowen's arguments against them. Second, I will present a further consideration that both clarifies the text of the fragment and also removes the most serious problem raised by Burkert. The upshot of both these points is to increase the likelihood that the fragment is authentic.

I reproduce the text of just the first part of the fragment as given in DK followed by the text as it appears in the two primary sources, Nicomachus and Porphyry.

DK i. 431-2

καλώς μοι δοκοῦντι τοὶ περὶ τὰ μαθήματα διαγνώμεναι, καὶ οὐθὲν ἄτοπον ὀρθῶς αὐτούς, οἶά ἐντι, περὶ ἑκάστων φρονέειν· περὶ γὰρ τᾶς τῶν ὅλων φύσιος καλῶς διαγνόντες ἔμελλον καὶ περὶ τῶν κατὰ μέρος, οἶά ἐντι, καλῶς ὀψεῖσθαι. περί τε δὴ τᾶς τῶν ἄστρων ταχυτᾶτος καὶ ἐπιτολᾶν καὶ δυσίων παρέδωκαν ἄμῖν σαφῆ διάγνωσιν καὶ περὶ γαμετρίας καὶ ἀριθμῶν καὶ σφαιρικᾶς καὶ οὐχ ἤκιστα περὶ μωσικᾶς. ταῦτα γὰρ τὰ μαθήματα δοκοῦντι ἦμεν ἀδελφεά· περὶ γὰρ ἀδελφεὰ τὰ τῶ ὅντος πρώτιστα δύο εἴδεα τὰν ἀναστροφὰν ἔχει. πρᾶτον μὲν οὖν ἐσκέψαντο, ὅτι οὐ δυνατόν ἐστιν ἦμεν ψόφον μὴ γενηθείσας πληγᾶς τινων ποτ' ἄλλαλα. (The fragment continues)

Nic. *Arith.* p. 6.16–7.5 (Hoche)

άλλὰ καὶ ᾿Αρχύτας ὁ Ταραντῖνος ἀρχόμενος τοῦ ἀρμονικοῦ τὸ αὐτὸ οὕτω πως λέγει καλῶς μοι δοκοῦντι περὶ τὰ μαθήματα διαγνώμεναι καὶ οὐδὲν ἄτοπον αὐτοὺς ὀρθῶς, οἶά ἐντι, περὶ ἑκάστου φρονέειν. περὶ γὰρ τᾶς τῶν ὅλων φύσιος καλῶς διαγνόντες ἔμελλον καὶ περὶ τῶν κατὰ μέρος, οἶά ἐντι, καλῶς ὀψεῖσθαι· περί τε δὴ τᾶς γεωμετρικᾶς καὶ ἀριθμητικᾶς καὶ σφαιρικᾶς παρέδωκαν ἄμμιν σαφῆ διάγνωσιν, οὐχ ῆκιστα δὲ καὶ περὶ μουσικᾶς. ταῦτα γὰρ τὰ μαθήματα δοκοῦντι ἔμμεναι ἀδελφεά· περὶ γὰρ ἀδελφεὰ τὰ τοῦ ὄντος πρώτιστα δύο εἴδεα τὰν ἀναστροφὰν ἔχει. καὶ Πλάτων δὲ ἐπὶ τέλει τοῦ τρισκαιδεκάτου τῶν νόμων...

Por. in Ptol. Harm. p. 56 (During)

παρακείσθω δὲ καὶ νῦν τὰ ᾿Αρχύτα τοῦ Πυθαγορείου, οὖ μάλιστα καὶ γνήσια λέγεται εἶναι τὰ συγγράμματα. λέγει δ᾽ ἐν τῷ Περὶ μαθηματικῆς εὐθὺς ἐναρχόμενος τοῦ λόγου τάδε·

"Καλῶς μοι δοκοῦντι τοὶ περὶ τὰ μαθήματα διαγνῶναι καὶ οὐθὲν ἄτοπον ὀρθῶς αὐτοὺς περὶ ἐκάστου θεωρεῖν. περὶ γὰρ τᾶς τῶν ὅλων φύσιος καλῶς διαγνόντες ἔμελλον καὶ περὶ τῶν κατὰ μέρος, οἶά ἐντι, ὅψεσθαι. περί τε δὴ τᾶς τῶν ἄστρων ταχυτᾶτος καὶ ἐπιτολᾶν καὶ δυσίων παρέδωκαν ἁμῖν διάγνωσιν καὶ περὶ γαμετρίας

¹ Walter Burkert, *Lore and Science in Ancient Pythagoreanism*, tr. Edwin Minar (Cambridge, Mass., 1972), pp. 379–80 n. 46. A. C. Bowen, 'The Foundations of Early Pythagorean Harmonic Science: Archytas, Fragment 1', *Ancient Philosophy* II, 2 (1982), pp. 79–104.

καὶ ἀριθμῶν καὶ οὐχ ἥκιστα περὶ μουσικᾶς. ταῦτα γὰρ τὰ μαθήματα δοκοῦντι ἡμεν ἀδελφεά. πρᾶτον μὲν οὖν ἐσκέψαντο, ὅτι οὐ δυνατόν ἐστιν ἡμεν ψόφον μὴ γενηθείσας πληγᾶς τινων ποτ' ἄλλαλα. πλαγὰν δ' ἔφαν γίνεσθαι, ὅκκα...(the fragment continues).

Individual sentences from the fragment are also quoted in Iamblichus but they are irrelevant for present purposes (see DK i. 431).

It seems to me that while most of Bowen's attempts to respond to Burkert's doubts miss the mark, in one important case he is successful. Burkert had noticed that as the text is presented in DK the enumeration of $\mu a \theta \dot{\eta} \mu a \tau a$ in the fragment is strangely redundant. First there is mention of knowledge $\pi\epsilon\rho i$ $\tau\epsilon$ $\delta\dot{\gamma}$ $\tau\hat{a}s$ $\tau\hat{\omega}\nu$ $\tilde{a}\sigma\tau\rho\omega\nu$ $\tau a\chi v\tau\hat{a}\tau os$ καὶ ἐπιτολᾶν καὶ δυσίων and then of knowledge περὶ γαμετρίας καὶ ἀριθμῶν καὶ σφαιρικάς καὶ οὐχ ηκιστα περὶ μωσικάς (DK i. 432, 4-7). The difficulty is that it is hard to see what difference there is between investigation of the speeds, risings, and settings of stars and the field of σφαιρικά. Bowen finds a neat solution to this dilemma by pointing out that the text of the passage in DK is a combination of the versions of the two sources for the text, Porphyry and Nicomachus. Only Nicomachus mentions σφαιρικά. In fact several features of Nicomachus' version (περί τε δη τας γεωμετρικάς καὶ ἀριθμητικᾶς καὶ σφαιρικᾶς παρέδωκαν ἄμμιν σαφῆ διάγνωσιν, οὐχ ῆκιστα δὲ καὶ περὶ μουσικάς) are suspicious (as Bowen points out) and look rather like Nicomachus' own rewriting of the passage in later terminology.² We should thus accept the version of the passage which is given by Porphyry ($\pi\epsilon\rho i \tau \epsilon \delta \dot{\eta} \tau \hat{a}_s \tau \hat{\omega} \nu$ ἄστρων ταχυτάτος καὶ ἐπιτολάν καὶ δυσίων παρέδωκαν ἁμῖν διάγνωσιν καὶ περὶ γαμετρίας καὶ ἀριθμῶν καὶ οὐχ ἥκιστα περὶ μουσικᾶς) with the addition of σαφῆ before διάγνωσιν, which is suggested by Nicomachus' version.3

However, this resolves just one of the difficulties with the fragment, and not the most important one at that. The most serious problem concerns the sentence $\pi \epsilon \rho i \gamma \dot{\alpha} \rho$ άδελφεὰ τὰ τῶ ὄντος πρώτιστα δύο εἴδεα τὰν ἀναστροφὰν ἔχει (DK i. 432, 8-9; underlined above). This sentence immediately follows upon the assertion that the $\mu a\theta \dot{\eta} \mu a \tau a$ which Archytas lists are $\dot{a}\delta \epsilon \lambda \phi \epsilon \dot{a}$ and provides an argument for that assertion. They are sister sciences because 'they are concerned with the two foremost kinds of being'. At first sight what the 'two foremost kinds' of being might be seems rather a puzzle. There is no evidence elsewhere for Archytas having postulated two primary kinds of being nor does the phrase seem explicable in terms of any philosophical system of the fifth or fourth century including Plato and Aristotle. However, if we read the pages in Nicomachus which immediately precede the quotation of the Archytas fragment the answer becomes clear. Nicomachus bases his own account of the $\mu a\theta \dot{\eta} \mu a \tau a$ on two basic kinds of being, $\pi \lambda \hat{\eta} \theta o_S$ and $\mu \dot{\epsilon} \gamma \epsilon \theta o_S$ (Ar. 1.2ff.). He specifically refers to them as $\delta \acute{v}o$ $\epsilon \ifmmode{i} \delta \eta \end{tabular}$ at Ar. 4.20. Thus it is likely that the two foremost kinds of being mentioned in the Archytas fragment are $\pi\lambda\hat{\eta}\theta_{0S}$ and $\mu \acute{\epsilon} \gamma \epsilon \theta$ os. Since the only parallel for this idea is found much later than Archytas in Nicomachus, the fragment begins to look very suspect.4

Bowen's response to this difficulty goes astray. He argues that Plato and Aristotle did distinguish between $\pi\lambda\hat{\eta}\theta os$ and $\mu\epsilon\gamma\epsilon\theta os$ in many places (e.g. Charmides 118 b 2–8). However, the point is surely that neither Plato nor Aristotle made this a

² See Bowen, pp. 84-5.

³ See Bowen in his text.

⁴ See Burkert, p. 380 n. 46.

⁵ Bowen, p. 85. He says that the distinction between multitude and magnitude was 'commonplace in fifth and fourth century thought'. This is surely true, but it was *not* commonplace to call multitude and magnitude the primary two kinds of what is.

fundamental distinction in his metaphysics nor do they give any indication that any other thinker had done so. If the text as DK presents it were acceptable, this mention of the two primary kinds of being would be very strong evidence against its authenticity.

However, we only have to compare the two primary sources for the text to see the solution to the problem. The entire offending sentence $(\pi\epsilon\rho \hat{\iota})$ $\gamma \hat{a}\rho$ $\hat{a}\delta\epsilon\lambda\phi\epsilon\hat{a}$ $\tau\hat{a}$ $\tau\hat{\omega}$ $\delta\nu\tau\sigma_S$ $\pi\rho\hat{\omega}\tau\iota\sigma\tau a$ $\delta\hat{\nu}o$ $\epsilon\hat{i}\delta\epsilon a$ $\tau\hat{a}\nu$ $\hat{a}\nu a\sigma\tau\rho o\phi\hat{a}\nu$ $\hat{\epsilon}\chi\epsilon\iota$) only occurs in Nicomachus. It is not found in Porphyry. It is thus clear that the sentence which is so closely tied to Nicomachus' own views propounded only a few pages earlier must have been inserted by Nicomachus to explain the preceding sentence of Archytas $(\tau a\hat{\nu}\tau a$ $\gamma\hat{a}\rho$ $\tau\hat{a}$ $\mu a\theta\hat{\eta}\mu a\tau a$ $\delta o\kappa o\hat{\nu}\nu\iota$ $\hat{\eta}\mu\epsilon\nu$ $\hat{a}\delta\epsilon\lambda\phi\epsilon\hat{a}$) in Nicomachean terms. This suggestion receives even further support when we realise that the sentence in question is the last line of Archytas (if it is Archytas) that Nicomachus quotes. Only Porphyry gives the rest of the fragment. Thus the truth would appear to be that the last line of Archytas that Nicomachus actually quoted was the assertion that the sciences are sisters. The explanation of this assertion in terms of two kinds of being belongs to Nicomachus.

The grammar and style of the offending sentence also show that it does not fit with the rest of the quotation and must be a remark of Nicomachus. First, in the immediately preceding sentence $\tau \dot{\alpha} \mu a \theta \dot{\eta} \mu a \tau a$ takes the plural verb $\delta o \kappa o \hat{\nu} \nu \tau \iota$ whereas in the sentence in question $\tau \dot{\alpha} \mu a \theta \dot{\eta} \mu a \tau a$ (understood) has the singular $\xi \chi \epsilon \iota$ as its verb. Such inconsistency in two successive sentences is not easily ascribed to a single author. The singular is standard grammar and what we would expect from Nicomachus. Second, the meaning of $d\nu a \sigma \tau \rho o \phi \dot{\eta}$ found in the expression $\tau \dot{\alpha} \nu \dot{\alpha} \nu a \sigma \tau \rho o \phi \dot{\alpha} \nu \dot{\epsilon} \chi \epsilon \iota = '$ is concerned with' finds most parallels in the Hellenistic period or later. True, to judge from the word index in Hoche's edition of Nicomachus, the phrase is not used elsewhere in the Introduction to Arithmetic, but the entries in LSJ for the second major range of meanings of $d\nu a \sigma \tau \rho o \phi \dot{\eta}$ (dwelling, mode of life, occupation or concern) refer mainly to authors such as Polybius, Plutarch, and Philodemus. Thus both the philosophical sense of the sentence and its grammar and style show that it can be confidently ascribed to Nicomachus and not Archytas.

But, it might be objected, the offending sentence is in Doric and thus can hardly be the work of Nicomachus. However, the context of the fragment in Nicomachus is such that it is not implausible that a scribe would have 'corrected' the sentence by putting it into Doric. None of the changes presuppose any profound knowledge of Greek dialects. The sentence in question is a one-line statement that follows immediately on the quotation in Doric from Archytas and is in turn immediately followed by another sentence that refers to Plato by name in its first words. Not understanding that the sentence is Nicomachus' own comment on Archytas the scribe assumes that the Archytas fragment must continue up to the mention of Plato which begins the next line and accordingly puts Nicomachus' one-line comment into Doric.

At this point the two most problematic aspects of the fragment have been addressed. A few difficulties remain, but once the primary reason for doubt is removed they are not enough to constitute serious doubt of the fragment's authenticity.

The first point is that half the fragment is taken up with Archytas' reports of his predecessors' findings in indirect discourse. The problem is not just that Archytas thus appears as the 'mere transmitter of Pythagorean wisdom' but also that this is the role that Archytas is assigned in the apocryphal tradition that portrays him as locating texts of Ocellus for Plato (D. L. 8.80). Thus, it might appear that Fragment 1 is a forged

⁶ Bowen keeps the line in his text.

document portraying Archytas in the same role of transmitter as he played regarding the texts of Ocellus.⁷ Such a point could be used to support other stronger evidence for spuriousness, but it is too weak to stand on its own. There are parallels for similar praise of predecessors (Hippoc. *Vict.* 1.1, *Hebd.* 53).⁸

Most serious is the doubt raised by the close correspondence between the sentence on 'sister sciences' in Archytas (ταῦτα γὰρ τὰ μαθήματα δοκοῦντι ἡμεν ἀδελφεά) and Republic 530d (καὶ αὖται ἀλλήλων ἀδελφαί τινες αἱ ἐπιστῆμαι εἶναι [sc. κινδυνεύουσι], ώς οῗ τε Π υθαγόρειοί φασι...). In Archytas the 'sister sciences' are the quadrivium, while in Plato the reference is most immediately to astronomy and harmonics.9 Given the similarity between the passages it is possible to see the influence going either way. However, the point is that it is amazing if just this text of Archytas which Plato is referring to should be preserved. Such a coincidence might lead us to suspect that someone forging in the name of Archytas drew this line directly out of Plato. Plato assigns the idea to Pythagoreans, so the forger sees this as something safe to admit into his work by 'Archytas'. 10 Once again this point has some force, but it is only conclusive if there are other features of the fragment that betray the forger. If the fragment otherwise avoids the sophisticated Platonic and Aristotelian terminology that is typical of the pseudo-Pythagorean literature, the similarity with the Republic is best explained as a result of Plato's having read this passage of Archytas, however great the coincidence that just this bit of Archytas should be preserved.11

The remaining difficulty concerns the use of the word $\mu a \theta \dot{\eta} \mu a \tau a$ in the fragment. Burkert argues that it is a post-Platonic usage. It would thus be the type of linguistic evidence that would indicate that we are dealing with a pseudo-Pythagorean writing and would provide the background in which the correspondence with the *Republic* discussed above would be suspicious. But how clear is it that $\mu a \theta \dot{\eta} \mu a \tau a$ is used in a post-Platonic sense?

Generally speaking Plato uses $\mu \dot{\alpha} \theta \eta \mu a$ to refer to any sort of study and not just the mathematical studies that became the quadrivium (arithmetic, geometry, astronomy, and music). However, in *Republic* VII Plato already gives special status to certain $\mu a \theta \dot{\eta} \mu a \tau a$, and in the *Laws* (817e) he refers to a special group of $\tau \rho \dot{\alpha} a \mu a \theta \dot{\eta} \mu a \tau a$ (= arithmetic, geometry, and astronomy). Even more pertinent is the fact that at *Theaetetus* 145a Theodorus is portrayed as teaching the quadrivium of geometry, astronomy, harmony, and arithmetic. Unless Plato is being wildly anachronistic, it appears that already at the end of the fifth century four $\mu a \theta \dot{\eta} \mu a \tau a$ had a special status of some sort. It is true that a technical sense of $\mu a \theta \dot{\eta} \mu a \tau a$ referring to a set body of mathematical studies does appear in the post-Platonic *Epinomis*. However, those referred to in Archytas fit Plato's description of Theodorus better than the system presented in the *Epinomis*. The $\mu a \theta \dot{\eta} \mu a \tau a$ in the *Epinomis* are more extensive than the quadrivium, including stereometry and dialectic as well. If the Archytas fragment were closely tied to Platonic doctrine, and if it is even supposed to have

⁷ Burkert, pp. 379–80 n. 46. Bowen, p. 83 seems to think that Burkert's point is that Archytas assumes two roles in the fragment, one as a transmitter of wisdom of his predecessors and another as an independent theorist.

⁸ Burkert, pp. 379-80 n. 46.

⁹ Bowen, p. 84, makes the good point, however, that Plato thinks that 'all the sciences... reach fruition only in the understanding of their dependence and kinship'. It would thus appear that Plato could call all the sciences $\mathring{a}\delta\epsilon\lambda\phi\epsilon\acute{a}$ as Archytas does.

¹⁰ Burkert, p. 380 n. 46.

¹¹ The fact that it is the beginning of Archytas' book is one major reason that it has been preserved.

drawn the statement about sister sciences from *Republic* VII, it is odd that neither stereometry nor dialectic is mentioned.

In the end, however, the point about the use of $\mu a\theta \dot{\eta} \mu a\tau a$ is most seriously undercut by the difficulty of determining who influenced whom. Archytas was a contemporary of Plato and it is very difficult to clarify the lines of influence between them. Surely it is not impossible that Archytas already regarded certain studies (= the quadrivium) as primary and referred to them as the $\mu a\theta \dot{\eta} \mu a\tau a$, especially since all our testimonia suggest that his work concentrated on just these areas (geometry A14, music A16 and 19, arithmetic A19–21).¹²

Thus all the doubts about the fragment which remain after the text is clarified turn out to be, at best, inconclusive. Furthermore, we must balance against these doubts other points which speak for authenticity. First, it should be noted that when compared to the free use of Platonic and Aristotelian terminology in the numerous texts forged in Archytas' name the use of at most one such questionable term in Fr. 1 looks insignificant. The goal of most of the forgeries is to assign Platonic and Aristotelian concepts wholesale to the earlier Pythagoreans. Second, it is significant that the description of astronomy given in Archytas Fr. 1 is of an empirical astronomy concerned with risings and settings which shows no influence of the programme for astronomy set out by Plato in the *Republic*. Such a description of astronomy is unlikely to have occurred in a post-Platonic forgery. 13

It is hard to feel totally confident in asserting the authenticity of any Pythagorean text given the amount of forgery in the tradition. However, once the text of Fr. 1 of Archytas has been clarified there do not appear to be any serious doubts about its authenticity.¹⁴

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- ¹² Indeed, another passage in Burkert's book seems to suggest that he recognises that the use of $\mu a \theta \dot{\eta} \mu a \tau a$ is not a good means of determining the authenticity of the fragment for the very reason which I have just given: 'The question of the extent to which Pythagoreans anticipated Plato in the treatment of the four branches and the development of the concept of the $\mu a \theta \dot{\eta} \mu a \tau a$ depends on the genuineness of the long fragment of Archytas' (p. 422 and n. 123).
- ¹³ Burkert himself draws attention to two such points. First, 'the lack of clarity about the concept of speed (rapidity of propagation or frequency of vibration)' makes the fragment a good target of Theophrastus' polemic (fr. 89). Second, the laborious enumeration of different pieces of evidence $(\sigma\eta\mu\epsilon\hat{\iota}\alpha)$ in the latter half of the fragment also suggests authenticity.
- ¹⁴ I would like to thank Myles Burnyeat and Walter Burkert for reading an earlier draft of this paper and for providing helpful comments.